

LABORATORY GUIDE

Linear Flexible Joint with Inverted Pendulum Experiment for LabVIEW™ Users

Developed by: Jacob Apkarian, Ph.D., Quanser Hervé Lacheray, M.A.SC., Quanser Peter Martin, M.A.SC., Quanser



CAPTIVATE. MOTIVATE. GRADUATE.

© 2012 Quanser Inc., All rights reserved.

Quanser Inc. 119 Spy Court Markham, Ontario L3R 5H6 Canada info@quanser.com Phone: 1-905-940-3575

Fax: 1-905-940-3576

Printed in Markham, Ontario.

For more information on the solutions Quanser Inc. offers, please visit the web site at: http://www.quanser.com

This document and the software described in it are provided subject to a license agreement. Neither the software nor this document may be used or copied except as specified under the terms of that license agreement. All rights are reserved and no part may be reproduced, stored in a retrieval system or transmitted in any form or by any means, electronic, mechanical, photocopying, recording, or otherwise, without the prior written permission of Quanser Inc.

CONTENTS

1	Introduction Background		4
2			5
	2.1	Modeling	5
	2.2	Control	8
3	Lab Experiments		11
	3.1	Simulation	11
	3.2	Implementation	13
4	System Requirements		15
	4.1	Overview of Files	16
	4.2	Setup for Simulation	16
	43	Setup for Running on LEJC-PEN	17



1 INTRODUCTION

This laboratory manual describes how to design a state-feedback control system that can balance an inverted pendulum mounted on the linear flexible joint cart while minimizing the spring deflection.

The plant has two main components: the Quanser IP02 linear motion plant and the Quanser LFJC-PEN-E module.

Topics Covered

- Obtain a state-space representation of the open-loop system.
- Design and tune an LQR-based state-feedback controller satisfying the closed-loop system's desired design specifications.
- Simulate the system and ensure it is stabilized using the designed state-feedback control.
- Implement the state-feedback controller on the LFJC-PEN system and evaluate its actual performance.

Prerequisites

In order to successfully carry out this laboratory, the user should be familiar with the following:

- 1. See the system requirements in Section 4 for the required hardware and software.
- 2. Modeling and state-space representation.
- 3. State-feedback design using Linear-Quadratic Regular (LQR) optimization.
- 4. Basics of LabVIEWTM .
- 5. LabVIEW Integration lab detailed in Appendix A in the IP02 Lab Workbook [2].

2 BACKGROUND

2.1 Modeling

2.1.1 Model Convention

The single inverted pendulum and linear flexible joint cart model is shown in Figure 2.1. The LFJC-PEN module is coupled to the IP02 Linear Servo Base Unit through a linear spring with equivalent stiffness K_s . The positive sense of linear displacement is to the right when facing the cart. The positive sense of rotation of the pendulum is defined to be counter-clockwise (CCW), when facing the cart pinions. Finally, the zero angle, α = 0, of the pendulum corresponds to inverted pendulum perfectly vertical pointing upwards.

The IP02 cart location is at linear position x_c , while the LFJC-PEN cart is located at x_{jc} . The IP02 cart assembly has mass, m_c , and is actuated by an applied force, F_c . The total mass of the flexible joint cart and pendulum assembly is m_{jc} . The IP02 and LFJC-PEN carts have equivalent damping terms, B_{eq} , and $B_{eq_{jc}}$, respectively. The mass of the pendulum is defined as, m_p , with damping, B_p , located at the pendulum centre of mass, (x_p, y_p) . The distance from the pendulum pivot to the centre of mass of the pendulum is l_p .

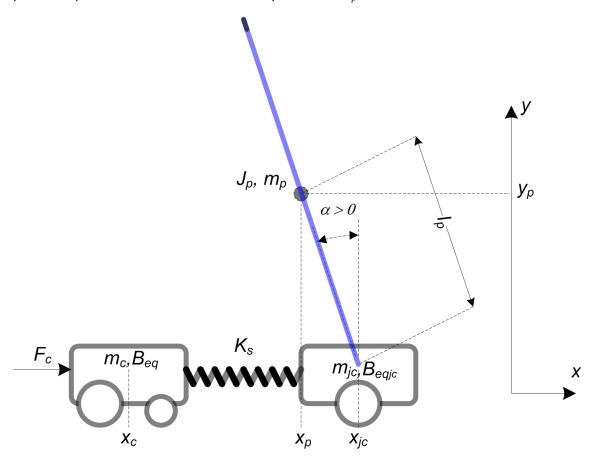


Figure 2.1: Linear flexible joint cart and single inverted pendulum conventions

2.1.2 Nonlinear Equations of Motion

Instead of using classical mechanics, the Lagrange method is used to find the equations of motion of the system. This systematic method is often used for more complicated systems such as robot manipulators with multiple joints.



The equations that describe the motions of the IP02 cart, the LFJC cart, and the pendulum with respect to the servo motor voltage, i.e. the dynamics, will be obtained using the Euler-Lagrange equation:

$$\frac{\partial^2 L}{\partial t \partial \dot{q}_i} - \frac{\partial L}{\partial q_i} = Q_i$$

The variables q_i are called *generalized coordinates*. For this system let

$$q(t)^{\top} = \begin{bmatrix} x_c(t) & x_{jc} & \alpha \end{bmatrix}$$

where, as shown in Figure 2.1, $x_c(t)$ is the IP02 cart position, x_{jc} is the LFJC cart position, and $\alpha(t)$ is the pendulum angle. The corresponding velocities are

$$\dot{q}(t)^{\top} = \begin{bmatrix} \frac{\partial x_c(t)}{\partial t} & \frac{\partial x_{jc}(t)}{\partial t} & \frac{\partial \alpha(t)}{\partial t} \end{bmatrix}$$

Note: The dot convention for the time derivative will be used throughout this document, e.g., $\dot{\alpha} = \frac{d\alpha}{dt}$. The time variable t will also be dropped from α , x_{jc} and x_c , i.e., $\alpha = \alpha(t)$.

With the generalized coordinates defined, the Euler-Lagrange equations for the rotary pendulum system are

$$\begin{split} \frac{\partial^2 L}{\partial t \partial \dot{x}_c} - \frac{\partial L}{\partial x_c} &= Q_1 \\ \frac{\partial^2 L}{\partial t \partial \dot{x}_{jc}} - \frac{\partial L}{\partial x_{jc}} &= Q_2 \\ \frac{\partial^2 L}{\partial t \partial \dot{\alpha}} - \frac{\partial L}{\partial \alpha} &= Q_3 \end{split}$$

The Lagrangian of the system is described

$$L = T - V$$

where T is the total kinetic energy of the system and V is the total potential energy of the system. Thus the Lagrangian is the difference between a system's kinetic and potential energies.

The generalized forces Q_i are used to describe the non-conservative forces (e.g., friction) applied to a system with respect to the generalized coordinates. In this case, the generalized force acting on the IP02 cart is

$$Q_1 = F_c - B_{eq}\dot{x_c},\tag{2.1}$$

the force acting on the LFJC cart is

$$Q_2 = -B_{eq_{ic}}\dot{x}_{jc},\tag{2.2}$$

and the force acting on the pendulum is

$$Q_3 = -B_p \dot{\alpha}. \tag{2.3}$$

The Euler-Lagrange equations is a systematic method of finding the equations of motion, i.e., EOMs, of a system. Once the kinetic and potential energy are obtained and the Lagrangian is found, then the task is to compute various derivatives to get the EOMs. After going through this process, the nonlinear equations of motion for the system can be obtained. See the supplied Maple worksheet (or its equivalent HTML representation) for the complete derivation.

Based on the system schematic shown in Figure 2.1 and the generalized forces Equation 2.1, Equation 2.2, and Equation 2.3, the first Lagrange equation can be expressed as:

$$m_c \ddot{x_c} - K_s(x_{jc} + x_c) = F_c - B_{eq} \dot{x_c},$$

the second Lagrange equation is

$$m_p l_p \sin(\alpha) \dot{\alpha}^2 - m_p l_p \cos(\alpha) \ddot{\alpha} + (m_{ic} + m_p) \ddot{x}_{ic} + K_s (x_{ic} - x_c) = -B_{eg_{ic}} \dot{x}_{ic}$$

and the third Lagrange equation is

$$m_p l_p^2 \ddot{\alpha} - m_p l_p \ddot{x}_{jc} \cos(\alpha) - m_p l_p g \sin(\alpha) = -B_p \dot{\alpha}$$

Solving the three Lagrange equations for the second-order time derivative of the Lagrangian coordinates results in the following non-linear equations:

$$\begin{split} \ddot{x_c} &= \frac{1}{m_c} \bigg(-B_{eq} \dot{x_c} - K_s x_c + K_s x_{jc} + F_c \bigg), \\ \ddot{x}_{jc} &= \frac{1}{-m_p + m_p \cos(\alpha)^2 - m_{jc}} \bigg(m_p \sin(\alpha) l_p \dot{\alpha}^2 + \frac{\cos(\alpha) B_p \dot{\alpha}}{l_p} + B_{eq_{jc}} \dot{x}_{jc} - K_s x_c + K_s x_{jc} - \cos(\alpha) m_p g \sin(\alpha) \bigg), \\ \text{and} \\ \ddot{\alpha} &= \frac{1}{-m_p + m_p \cos(\alpha)^2 - m_{jc}} \bigg(m_p \cos(\alpha) \sin(\alpha) \dot{\alpha}^2 + \frac{(B_p m_p + B_p m_{jc}) \dot{\alpha}}{l_p^2 m_p} + \frac{\cos(\alpha) B_{eq_{jc}} \dot{x}_{jc}}{l_p} - \frac{\cos(\alpha) K_s x_c}{l_p} \\ &+ \frac{\cos(\alpha) K_s x_{jc}}{l_p} + \frac{-m_p^2 g \sin(\alpha) l_p - m_p g \sin(\alpha) l_p m_{jc}}{l_p^2 m_p} \bigg) \end{split}$$

The force applied to the linear cart, F_c , is generated by the servo motor as described by the equation

$$F_c = \frac{\eta_g K_g K_t}{R_m r_{mp}} \left(-\frac{K_g K_m \dot{x_c}}{r_{mp}} + \eta_m V_m \right)$$
 (2.4)

See [1] for a description of the corresponding IP02 parameters (e.g. such as the back-emf constant, K_m).

2.1.3 Linearizing

Here is an example of how to linearize a two-variable nonlinear function called f(z). Variable z is defined

$$z^{\top} = [z_1 \ z_2]$$

and f(z) is to be linearized about the operating point

$$z_0^{\top} = [a \ b]$$

The linearized function is

$$f_{lin} = f(z_0) + \left(\frac{\partial f(z)}{\partial z_1}\right) \Big|_{z=z_0} (z_1 - a) + \left(\frac{\partial f(z)}{\partial z_2}\right) \Big|_{z=z_0} (z_2 - b)$$

2.1.4 Linear State-Space Model

The linear state-space equations are

$$\dot{x} = Ax + Bu \tag{2.5}$$

and

$$y = Cx + Du (2.6)$$



where x is the state, u is the control input, A, B, C, and D are state-space matrices. For the linear flexible joint cart and pendulum system, the state and output are defined

$$x^{\top} = \begin{bmatrix} x_c & x_s & \alpha & \dot{x_c} & \dot{x_s} & \dot{\alpha} \end{bmatrix}$$

and

$$y^{\top} = \begin{bmatrix} x_1 & x_2 & x_3 \end{bmatrix}.$$

where x_s is the variation in the linear spring length defined $x_s = x_{jc} - x_c$.

After linearizing the nonlinear equations of motion about the zero angle, and substituting the state given in Equation 2.1.4, we obtain the following state-space matrices:

$$A = \begin{bmatrix} 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & \frac{K_s}{m_c} & 0 & -\frac{B_{eq}}{m_c} & 0 & 0 \\ 0 & -\frac{K_s}{m_c} - \frac{K_s}{m_{jc}} & \frac{m_p g}{m_{jc}} & \frac{B_{eq}}{m_c} - \frac{B_{eq_{jc}}}{m_{jc}} & -\frac{B_{eq_{jc}}}{m_{jc}} & -\frac{B_p}{l_p m_{jc}} \\ 0 & -\frac{K_s}{l_p m_{jc}} & \frac{g(m_{jc} + m_p)}{l_p m_{jc}} & -\frac{B_{eq_{jc}}}{l_p m_{jc}} & -\frac{B_{eq_{jc}}}{l_p m_{jc}} & -\frac{B_p(m_{jc} + m_p)}{m_p l_p^2 m_{jc}} \end{bmatrix}$$

and

$$B = \begin{bmatrix} 0 \\ 0 \\ 0 \\ \frac{1}{m_c} \\ -\frac{1}{m_c} \\ 0 \end{bmatrix}.$$

In the output equation, the position of the IP02 cart, the LFJC cart, and pendulum angle are being measured. Based on this, the \mathcal{C} and \mathcal{D} matrices in the output equation are

$$C = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \end{bmatrix}$$
 (2.7)

and

$$D = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}. \tag{2.8}$$

Note: The velocities of the servos and pendulum angle can be computed in the digital controller, e.g., by taking the derivative and filtering the result though a high-pass filter.

2.2 Control

In Section 2.1, we found a linear state-state space model that represents the LFJC-PEN-E system. This model is used to investigate the stability properties of the system in Section 2.2.1. In Section 2.2.2, the notion of controllability is introduced. Using the Linear Quadratic Regular algorithm, or LQR, is a common way to find the control gain and is discussed in Section 2.2.3. Lastly, Section 2.2.4 describes the state-feedback control used to control the servo position while minimizing link deflection.

2.2.1 Stability

The stability of a system can be determined from its poles ([4]):

- Stable systems have poles only in the left-hand plane.
- Unstable systems have at least one pole in the right-hand plane and/or poles of multiplicity greater than 1 on the imaginary axis.
- Marginally stable systems have one pole on the imaginary axis and the other poles in the left-hand plane.

The poles are the roots of the system's characteristic equation. From the state-space, the characteristic equation of the system can be found using

$$\det(sI - A) = 0 \tag{2.9}$$

where det() is the determinant function, s is the Laplace operator, and I the identity matrix. These are the eigenvalues of the state-space matrix A.

2.2.2 Controllability

If the control input, u, of a system can take each state variable, x_i where $i = 1 \dots n$, from an initial state to a final state then the system is controllable, otherwise it is uncontrollable ([4]).

Rank Test The system is controllable if the rank of its controllability matrix

$$T = \left[B \ AB \ A^2 B \dots A^n B \right] \tag{2.10}$$

equals the number of states in the system,

$$rank(T) = n. (2.11)$$

2.2.3 Linear Quadratic Regular (LQR)

If (A,B) are controllable, then the Linear Quadratic Regular optimization method can be used to find a feedback control gain. Given the plant model in Equation 2.5, find a control input u that minimizes the cost function

$$J = \int_0^\infty x(t)' Q x(t) + u(t)' R u(t) dt,$$
 (2.12)

where Q and R are the weighting matrices. The weighting matrices affect how LQR minimizes the function and are, essentially, tuning variables.

Given the control law u = -Kx, the state-space in Equation 2.5 becomes

$$\dot{x} = Ax + B(-Kx)
= (A - BK)x$$

2.2.4 Feedback Control

The feedback control loop that in Figure 2.2 is designed to balance the pendulum by regulating the pendulum angle, α .

The reference state is defined

$$x_d = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

and the controller is therefore

$$u = -Kx, (2.13)$$



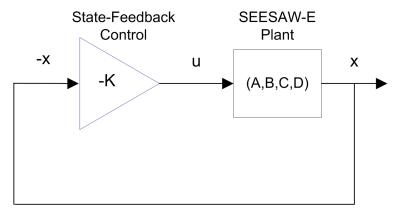


Figure 2.2: State-feedback control loop

which is the control used in the LQR algorithm.

To eliminate IP02 servo tracking error, we can augment the system to include an integrator such that

$$\dot{\eta} = \begin{bmatrix} A & 0 \\ 1 & 0 \end{bmatrix} \eta + \begin{bmatrix} B \\ 0 \end{bmatrix} u$$

where A and B are the state-space matrices defined in Section 2.1.4 and the states are

$$\eta^{\top} = \begin{bmatrix} x_c & x_{jc} & \alpha & \dot{x_c} & \dot{x}_j c & \dot{\alpha} & \int x_c \, \mathrm{d}t \end{bmatrix}$$

This introduces the integration terms $\eta_7(t)=\int \theta\,\mathrm{d}t$ to the feedback controller

$$u = K(-\eta).$$

3 LAB EXPERIMENTS

3.1 Simulation

In this section we will use the VI shown in Figure 3.1 to simulate the closed-loop control of the LFJC-PEN-E system. The system is simulated using the linear model summarized in Section 2.1. The VI uses the state-feedback control described in Section 2.2.4. The feedback gain K is found using the LQR command from the *Control Design and Simulation Toolkit* (LQR is described briefly in Section 2.2.3). The goal is to make sure the gain used successfully stabilizes the system (i.e., keeps it balanced), and does not saturate the dc motor.

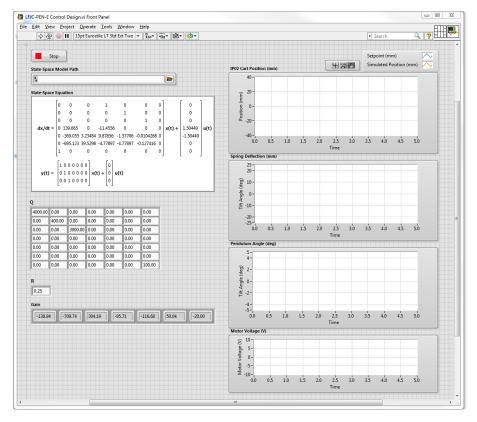


Figure 3.1: VI used to simulate LFJC-PEN-E.

IMPORTANT: Before you can conduct these experiments, you need to make sure that the lab files are configured according to your setup. If they have not been configured already, then you need to go to Section 4 to configure the lab files first.

3.1.1 Procedure

Follow these steps to simulate the system:

1. Open and run *LFJC-PEN-E Control Design.vi* as described in Section 4. Make sure you choose your model file using the *Model Path* control. The model file is generated using the *LFJC-PEN-E Modeling* VI by entering the state space model and exporting the resultant model file.



2. By default, the Q matrix is sent to identity matrix. Set the LQR weighting matrices to

and

$$R = 0.25$$
.

3. This automatically generates the gain

$$K = \begin{bmatrix} -138.93 & -709.32 & 304.16 & -95.71 & -116.64 & 50.05 & -20 \end{bmatrix}$$
.

LQR Tuning: When tuning the LQR, we start with the identity matrix. To put more emphasis on the IP02 cart position, and pendulum angle α , we set Q(1,1)=4000 and Q(3,3)=3000 respectively. The second diagonal element, Q(2,2) is set to 400 to regulate the spring deflection as a secondary control goal. Finally, a value of 100 is added to the last diagonal element, Q(7,7) as an integral gain for the IP02 cart to account for any steady-state error in the IP02 cart position.

4. Run the VI. The scopes should be displaying responses similar to Figure 3.2.

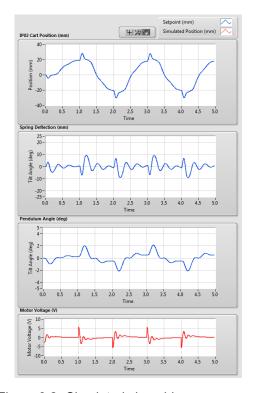


Figure 3.2: Simulated closed-loop response.

- 5. This is an iterative design process. You can update your Q and R matrices, and acquire a new control gain K on-the-fly.
- 6. Click on the STOP button to stop running the VI.

3.1.2 Analysis

As shown by the response in Figure 3.2, the pendulum maintains its balanced vertical position without saturating the motor voltage. Further analysis can be performed using the *Graph Palette*.

3.2 Implementation

The SEESAW Balance Control VI shown in Figure 3.3 is used to perform the balance control on the LFJC-PEN. The VI contains Quanser Rapid Control Prototyping Toolkit[®] blocks that interface with the dc motor and sensors of the LFJC-PEN system.

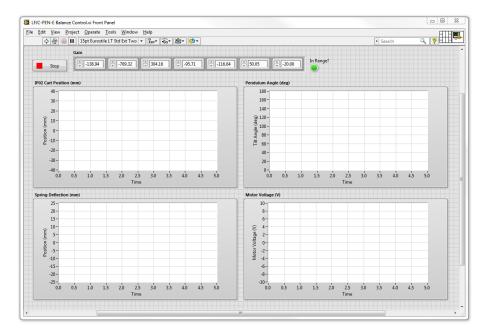


Figure 3.3: VI used to run controller on the LFJC-PEN.

IMPORTANT: Before you can conduct these experiments, you need to make sure that the lab files are configured according to your setup. If they have not been configured already, then you need to go to Section 4 to configure the lab files first.

3.2.1 Procedure

Follow this procedure:

- 1. Make sure gain K is set to the gain you found and simulated in Section 3.1.
- 2. Make sure that the pendulum is stationary in the downward (gantry) position, and the system is in the centre of the track.
- 3. Run the VI.
- 4. Once the model is running, manually bring the pendulum up to its upright vertical position. You should feel the motor voltage kick-in when it is within the range where the balance control engages. The scopes should be displaying responses similar to Figure 3.4.

Note: Once the controller has engaged, do not attempt to manually lower the pendulum. If the pendulum or carts move outside of a safe workspace, the system should halt the controller automatically.



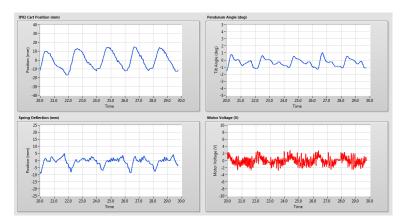


Figure 3.4: Typical response when balancing the LFJC-PEN system

5. To stop the experiment, click on the *Stop* button but **make sure you catch the pendulum before it swings down**.

3.2.2 Analysis

The balance control response is shown in Figure 3.5.

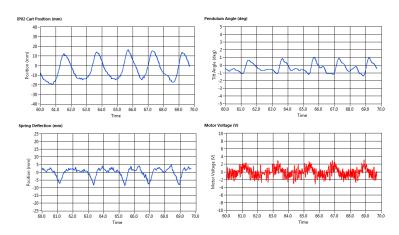


Figure 3.5: LFJC-PEN balance control response

Due to the friction in the system, the IP02 servo oscillates back-and-forth approximately ± 20 mm to balance the pendulum. The pendulum angle does not exceed 1.5 degrees when balanced, and the deflection of the spring does not exceed ± 10 mm. Because of the integrator, the IP02 cart eventually returns to the initial 0 mm setpoint.

4 SYSTEM REQUIREMENTS

Required Software

Make sure LabVIEWTM is installed with the following required add-ons:

- 1. LabVIEWTM
- 2. NI-DAQmx
- 3. NI LabVIEWTM Control Design and Simulation Module
- 4. NI LabVIEWTM MathScript RT Module
- 5. Quanser Rapid Control Prototyping Toolkit®

Note: Make sure the Quanser Rapid Control Prototyping (RCP) Toolkit is installed after LabVIEW. See the RCP Toolkit Quick Start Guide for more information.

Required Hardware

- Data acquisition (DAQ) device with 3x encoder inputs and that is compatible with Quanser Rapid Control Prototyping Toolkit[®].
- Quanser IP02 linear servo.
- Quanser LFJC-PEN-E (attached to the IP02).
- Quanser VoltPAQ-X1 power amplifier, or equivalent.

Before Starting Lab

Before you begin this laboratory make sure:

- LabVIEWTM is installed on your PC.
- DAQ device has been successfully tested (e.g., using the test software in the Quick Start Guide or the *Analog Loopback Demo*).
- LFJC-PEN-E and amplifier are connected to your DAQ board as described its User Manual [3].



4.1 Overview of Files

File Name	Description
LFJC-PEN-E User Manual.pdf	This manual describes the hardware of the LFJC-PEN system and explains how to setup and wire the system for the experiments.
LFJC-PEN-E Laboratory Manual.pdf	This document demonstrates how to obtain the linear state-space model of the system, simulate the closed-loop system, and implement controllers on the LFJC-PEN plant using LabVIEW TM .
LFJC-PEN-E Project.lvproj	LabVIEW project that contains all the VIs required for the lab.
LFJC-PEN-E Modeling.vi	VI used to generate the linear state-space model of the LFJC-PEN system.
LFJC-PEN-E Control Design.vi	VI used to design the LQR state-feedback gain and simulate the LFJC-PEN system.
LFJC-PEN-E Balance Control.vi	VI that implements the state-feedback control on the LFJC-PEN system.
LFJC-PEN-E.mws	Maple worksheet used to develop the model for the LFJC- PEN experiment. Waterloo Maple 9, or a later release, is required to open, modify, and execute this file.
LFJC-PEN-E.html	HTML presentation of the Maple Worksheet. It allows users to view the content of the Maple file without having Maple 9 installed. No modifications to the equations can be performed when in this format.

Table 4.1: Files supplied with the LFJC-PEN

4.2 Setup for Simulation

Before beginning the in-lab procedure outlined in Section 3.1, the modeling and control design VIs must must be configured.

Follow these steps:

- 1. Load LabVIEW™ .
- 2. Open the *LFJC-PEN-E Project.lvproj* LabVIEW project, shown in Figure 4.1.
- 3. Open the LFJC-PEN-E Modeling.vi shown in Figure 4.2.
- 4. The IP02 cart, LFJC cart and pendulum parameters are already set, by default. Run the VI to generate the linear state-space model.
- 5. In *Model Name*, enter the name of the model you and click on OK. This will save the state-space model under the folder *Model Files*. You can close this VI now.
- 6. Open the LFJC-PEN-E Control Design VI, shown in Figure 3.1.
- 7. Using the File Path control, select the model file.
- 8. Run the VI. The state-space model should load. You are now ready to design your LQR control and simulate the closed-loop response.

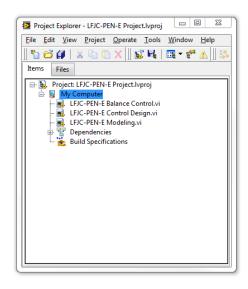


Figure 4.1: LabVIEW LFJC-PEN-E Project

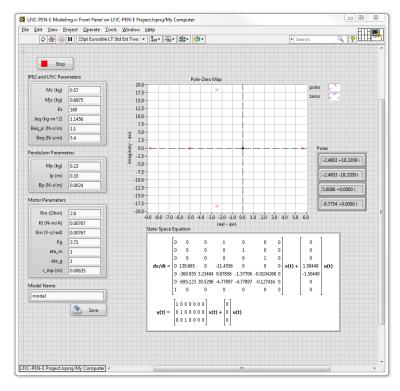


Figure 4.2: LFJC-PEN-E Modeling VI

4.3 Setup for Running on LFJC-PEN

Before performing the in-lab exercises in Section 3.2, the LFJC-PEN system and the *LFJC-PEN-E Balance Control.vi* must be configured properly.

Follow these steps to get the system ready for this lab:

- 1. Setup the IP02 with the LFJC-PEN module as detailed in the LFJC-PEN User Manual [3].
- 2. Make sure that the pendulum is stationary in the downward (gantry) position, and the system is in the centre of the track.
- 3. Open the LFJC-PEN-E Balance Control.vi, shown in Figure 3.3.
- 4. Set gain K control in the VI to the value found in Section 4.2 (or another gain you want to test on the system).
- 5. **Configure DAQ:** Ensure the HIL Initialize block is configured for the DAQ device that is installed in your system. To do this, go to the block diagram (CTRL-E) and double click on the **HIL Initialize** Express VI shown in Figure 4.3.

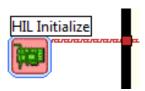


Figure 4.3: HIL Initialize Express VI

6. Under the Main tab, select the data acquisition device that is installed on your system in the *Board type* section. For example, in Figure 4.4 the Q8-USB is chosen.



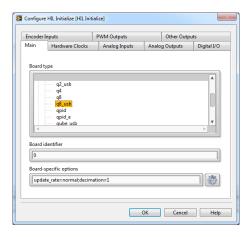


Figure 4.4: Select DAQ board that will be used to control system

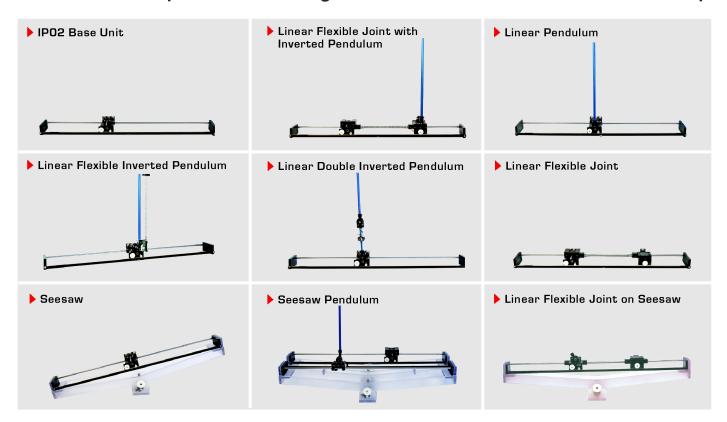
REFERENCES

- [1] Quanser Inc. IP02 User Manual, 2009.
- [2] Quanser Inc. IP02 Lab Workbook (LabVIEW), 2012.
- [3] Quanser Inc. SEESAW-E User Manual, 2012.
- [4] Norman S. Nise. Control Systems Engineering. John Wiley & Sons, Inc., 2008.



LFJC-PEN Laboratory Guide

Nine linear motion plants for teaching fundamental and advanced controls concepts



Quanser's linear collection allows you to create experiments of varying complexity – from basic to advanced. With nine plants to choose from, students can be exposed to a wide range of topics relating to mechanical and aerospace engineering. For more information please contact info@quanser.com

©2012 Quanser Inc. All rights reserved.

